

Appendix Tables

Appendix 1

$$\Psi_1 = \Psi_{200} \bar{\Psi}_{200}, \Psi_2 = \Psi_{200} \bar{\Psi}_{31-1}, \Psi_3 = \Psi_{200} \bar{\Psi}_{310}, \Psi_4 = \Psi_{200} \bar{\Psi}_{311}, \Psi_5 = \Psi_{31-1} \bar{\Psi}_{200}, \Psi_6 = \Psi_{310} \bar{\Psi}_{200},$$

$$\Psi_7 = \Psi_{311} \bar{\Psi}_{200}, \Psi_8 = \Psi_{31-1} \bar{\Psi}_{31-1}, \Psi_9 = \frac{1}{\sqrt{2}}(\Psi_{31-1} \bar{\Psi}_{31-0} + \Psi_{310} \bar{\Psi}_{31-1})$$

$$\Psi_{10} = \frac{1}{\sqrt{6}}(\Psi_{31-1} \bar{\Psi}_{311} + 2\Psi_{310} \bar{\Psi}_{310} + \Psi_{311} \bar{\Psi}_{31-1}), \Psi_{11} = \frac{1}{\sqrt{2}}(\Psi_{310} \bar{\Psi}_{311} + \Psi_{311} \bar{\Psi}_{310}), \Psi_{12} = \Psi_{311} \bar{\Psi}_{311}$$

$$\Psi_{13} = \frac{1}{\sqrt{2}}(\Psi_{310} \bar{\Psi}_{31-1} - \Psi_{31-1} \bar{\Psi}_{310}), \Psi_{14} = \frac{1}{\sqrt{2}}(\Psi_{311} \bar{\Psi}_{31-1} - \Psi_{31-1} \bar{\Psi}_{311}), \Psi_{15} = \frac{1}{\sqrt{2}}(\Psi_{311} \bar{\Psi}_{310} - \Psi_{310} \bar{\Psi}_{311}),$$

$$\Psi_{16} = \frac{1}{\sqrt{3}}(\Psi_{31-1} \bar{\Psi}_{311} - \Psi_{310} \bar{\Psi}_{310} + \Psi_{311} \bar{\Psi}_{31-1})$$

Appendix 2

$$\mathbf{P}_{1A} = 4X(E_1\mathbf{i} + E_2\mathbf{j} + E_3\mathbf{k}), \mathbf{P}_{2A} = (XE_1 + YE_2)\mathbf{i} + (YE_1 + XE_2)\mathbf{j} + 2XE_3\mathbf{k}, \mathbf{P}_{3A} = 2X(E_1\mathbf{i} + E_2\mathbf{j})$$

$$\mathbf{P}_{4A} = (XE_1 + YE_2)\mathbf{i} + (-YE_1 + XE_2)\mathbf{j} + 2XE_3\mathbf{k}, \{\mathbf{P}_{5A} = \mathbf{P}_{2A}, \mathbf{P}_{6A} = \mathbf{P}_{3A}, \mathbf{P}_{7A} = \mathbf{P}_{4A}\} = \text{Degenerates states,}$$

$$\mathbf{P}_{8A} = -2[(XE_1 - YE_2)\mathbf{i} + (-YE_1 + XE_2)\mathbf{j}], \mathbf{P}_{9A} = (-XE_1 - YE_2)\mathbf{i} + (YE_1 - XE_2)\mathbf{j} - 2XE_3\mathbf{k}$$

$$\mathbf{P}_{10A} = -2X(E_1\mathbf{i} + E_2\mathbf{j} + 4E_3\mathbf{k})/3, \mathbf{P}_{11A} = (-XE_1 + YE_2)\mathbf{i} + (-YE_1 - XE_2)\mathbf{j} - 2XE_3\mathbf{k}$$

$$\mathbf{P}_{12A} = -2[(XE_1 - YE_2)\mathbf{i} + (YE_1 + XE_2)\mathbf{j}], \mathbf{P}_{13A} = (-XE_1 + YE_2)\mathbf{i} + (YE_1 - XE_2)\mathbf{j} - 2XE_3\mathbf{k},$$

$$\mathbf{P}_{14A} = -2X(E_1\mathbf{i} + E_2\mathbf{j}), \mathbf{P}_{15A} = (-XE_1 + YE_2)\mathbf{i} + (-YE_1 - XE_2)\mathbf{j} - 2XE_3\mathbf{k}, \mathbf{P}_{16A} = -4X(E_1\mathbf{i} + E_2\mathbf{j} + E_3\mathbf{k})/3$$

with

$$X = \frac{d^2\omega_0 [\cos \omega_0 t - \cos \omega t]}{3\hbar [\omega^2 - \omega_0^2]}, Y = \frac{d^2\omega_0 [\omega_0 \sin \omega_0 t - \omega \sin \omega t]}{3\hbar [\omega^2 - \omega_0^2]}, d = -e \int_0^\infty R_{20} R_{31} r^3 dr$$

R_{20}, R_{31} are the radial functions, e represents the charge of a positron, and $\omega_0 = \omega_2 - \omega_1, \omega^2 \neq \omega_0^2$.

Appendix 3

Of the equation 37 the irreducible representation is $\Gamma_\pi = 2A_2 + 3B_2$, using the notation $N_1 = \phi_1, C_2 = \phi_2, C_3 = \phi_3, C_4 = \phi_4, C_5 = \phi_5$ and using the relationship projection operator

$$\hat{P}^j = \frac{l_j}{h} \sum_R \chi(R)^j \hat{R}$$

Where l_j represents the dimension of the group, we have:

$$\Psi_1^{A_2} = \frac{1}{\sqrt{2}} (\phi_2 - \phi_5)$$

$$\Psi_2^{A_2} = \frac{1}{\sqrt{2}} (\phi_3 - \phi_4)$$

$$\Psi_3^{B_2} = \phi_1$$

$$\Psi_4^{B_2} = \frac{1}{\sqrt{2}} (\phi_2 - \phi_5)$$

$$\Psi_5^{B_2} = \frac{1}{\sqrt{2}} (\phi_3 - \phi_4)$$